# Photothermal deflection studies of GaAs epitaxial layers

Nibu A. George, C. P. G. Vallabhan, V. P. N. Nampoori, and P. Radhakrishnan

Photothermal beam deflection studies were carried out with GaAs epitaxial double layers grow semi-insulating GaAs substrates. The impurity densities in thin epitaxial layers were found winds the effective thermal diffusivity of the entire structure. © 2002 Optical Society of America OCIS codes: 120.4290, 160.6000, 300.6430, 310.6870.

#### 1. Introduction

The absorption of intensity modulated optical radiation by a sample leads to periodic heat generation, thereby causing excitation of thermal waves in the sample. Thermal wave physics is emerging as a valuable tool in the study of thermal properties of materials, especially in the semiconductor industry. 1-5 Among the various methods for investing these thermal waves the photothermal deflection (PTD) technique possesses some unique characteristics and advantages compared with the other approaches. 5-7

The concept of light-beam deflection by thermally induced changes in the index of refraction of a medium has been known for a long time. However, only in did Boccara et al.8 demonstrated the use of photothermal beam deflection as a valuable tool in material characterization. In subsequent years, theoretical and experimental contributions by Jackson et al.9 in 1981, Aamodt and Murphy10 in 1981, and Grice et al.11 in 1983 formed a strong basis for this technique. The PTD technique is essentially based on detection of the refractive-index gradient associated with a temperature gradient. Absorption of optical radiation (the pump beam) results in the generation of thermal waves in a solid sample, which eventually generates a temperature gradient in a gas or a liquid that is in contact with the sample's surface. The refractive-index gradient associated with this temperature profile can be conveniently me tored by a second laser beam (the probe beam), who passes through the heated region, because the probability is deflected by the refractive-index gradient.

In the present paper we describe the use of the last of the last

In the present paper we describe the use of the? technique for the thermal characterization of & multilayer samples. Among the various experient tal approaches to evaluating the thermal diffusion of solids by use of PTD, the strategy that we use the present investigation is measurement of the? signal phase as a function of pump-probe offset a fixed modulation frequency. 6.12.13

## 2. Theory

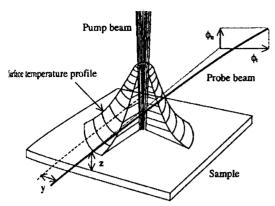
The PTD technique can be employed in various tection configurations for the investigation of a samples.6,7,14,15 Probe-beam deflection in the sa ming configuration is one of the widely accepted simple approaches among the PTD measure schemes. A schematic representation of the pri beam skimming configuration is shown as Fig. 1. this configuration the solid sample is irradiated a focused laser beam and the resultant refract index gradient generated in the coupling fluid ally a liquid) that is in contact with the sa surface is monitored with a low-power probe passing through this gradient. In this scheme assumed that the temperature distribution is coupling fluid located close to the sample suries the same as that which is located at the sample face. The probe beam propagating through the tially varying refractive-index gradient at deflection from its normal path, and the amount deflection is determined by a number of thermal optical parameters of the solid sample.

For a Gaussian beam propagating through a homogeneous medium, most of the beam parameters be deduced from the analysis made by Mandard Royce. 16 The propagation of a light in

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It 1. Schematic diagram of the probe-beam skimming PTD efection; y, z, the transverse and the vertical offsets, respective.

rough a spatially varying index of refraction is

$$\frac{\mathrm{d}}{\mathrm{d}s}\left(n_o\,\frac{\mathrm{d}r_o}{\mathrm{d}s}\right) = \nabla_{\perp}n(r,\,t),\tag{1}$$

the  $r_0$  is the perpendicular displacement of the ram from its original direction,  $n_0$  is the uniform star of refraction, and  $\nabla_{\perp} n(r,t)$  is the gradient of the ray of refraction perpendicular to the ray path. igation (2) can be integrated over the ray path:

$$\frac{\mathrm{d}r_o}{\mathrm{d}s} = \frac{1}{n_o} \int_{\mathrm{path}} \nabla_{\perp} n(r, t) \mathrm{d}s, \qquad (2)$$

were s is the optical path length. Because the destion is small, one can get the expression for the effection,  $\phi(t)$ , as

$$\frac{\mathrm{d}r_o}{\mathrm{d}s} = \phi(t) = \frac{1}{n_o} \frac{\partial n}{\partial T} \int_{-\infty} \nabla_{\perp} T(r, t) \mathrm{d}s, \qquad (3)$$

there  $\nabla_{\cdot} T(r,t)$  is the temperature gradient perpension to the ray path. Deflection  $\phi(t)$  can be rested into two components,  $\phi_n$  and  $\phi_t$ , where  $\phi_n$  and are, respectively, the deflections normal and parallel to the sample surface. Let the probe beam are a transverse offset y with respect to the pumpmaxis and a vertical offset z with respect to the suple surface. The temperature field distribution at is due to the pumpbeam absorption, obtained by without of the heat diffusion equations in the sample seel as in the coupling fluid, leads to the evaluation of  $\phi_t$  and  $\phi_n$  as  $^{13}$ 

$$\phi_{t} = -\frac{1}{\pi n} \frac{\mathrm{d}n}{\mathrm{d}T} \int_{0}^{\infty} \sin(\delta y) A \, \exp(-\beta_{0}z) \delta \mathrm{d}\delta$$

$$\times \exp(j\omega t), \qquad z > 0, \qquad (4)$$

$$\phi_{t} = -\frac{1}{\pi n} \frac{\mathrm{d}n}{\mathrm{d}T} \int_{0}^{x} \cos(\delta y) A \, \exp(-\beta_{0}z) \beta_{0} \mathrm{d}\delta$$

where A is a complex integration constant,  $\delta$  is a spatial Fourier-transformed variable, and  $\beta_0 = (\delta^2 + j\omega/D_0)^{1/2}$ , where  $D_0$  is the thermal diffusivity of the coupling fluid.

Salazar et al. analyzed various experimental conditions and arrived at expressions that describe a linear relationship of the PTD signal phase as well as of the amplitude to various parameters such as pump-probe offset and height of the probe beam above the sample surface. 17 For a = b = z = 0, where a, b, and z are the pump-beam spot size. The probe-beam spot size, and the probe-beam height above the sample surface, there is a linear relationship between the phase of the transverse component of the probe-beam deflection and the pump-probe This linearity is found to be valid for three offset. different configurations: (1) probe-beam skimming configuration with the pump and the probe beams on the same side of the sample, (2) probe-beam skimming configuration with the pump and the probe beams on opposite sides of the sample, and (3) the probe beam passing through the sample. The experimental configuration used in the present study is of the first type. In this configuration the slope of the plot connecting the phase of the PTD signal and the pump-probe offset is given by

$$m = \frac{1}{\mu_s} = (\pi f/\alpha_s)^{1/2}.$$
 (6)

Practically, the condition a = b = z = 0 cannot be achieved, and finite values of a, b, and z may result in a change in slope, especially when the sample possesses low thermal diffusivity. But, for samples with moderately high thermal diffusivity, Eq. (6) holds for finite values of a, b, and z.<sup>17,18</sup>

# 3. Experimental

N-type and p-type GaAs thin films grown upon semiinsulating GaAs substrates were used in the investigation. The thin films were grown by the molecular beam epitaxial method (Technical University of Eindhoven, Eindhoven, The Netherlands). All of the samples contained two epitaxial layers. The sample structure together with the specifications of each layer, including the growth conditions and dopants, are given in Table 1. For convenience we have labeled the samples arbitrarily 1, 2, 3, and 4.

Continuous-wave laser emission at 488 nm from an argon-ion laser (Liconix 5000) was used as the pump beam. The laser beam had a  $(1/e^2)$  diameter of 1.2 mm. In all the measurements a laser power of 50 mW (±0.5%) was used. Carbon tetrachloride (CCl<sub>4</sub>), which is the most suitable and most commonly used coupling fluid in photothermal deflection studies, was used as the coupling fluid to the sample. The significant parameters that make CCl<sub>4</sub> a good coupling fluid in the PTD technique are its low thermal diffusivity,  $\alpha = 7.31 \times 10^{-4} \, \mathrm{cm}^2 \, \mathrm{s}^{-1}$ , and its very high rate of change of refractive index with respect to temperature,  $(\mathrm{d}n/\mathrm{d}T) = 6.12 \times 10^{-4} \, \mathrm{K}^{-1}$ . 19

A schematic view of the experimental setup is de-

 $\times \exp(j\omega t)$ 

(5)

Table 1. Structure, Properties, and Growth Conditions of the Doped GaAs Epitaxial Layers upon the Semi-Insulating GaAs Substrate

Sample	$l (\mu m)^a$	n (cm <sup>-3</sup> ) <sup>b</sup>	T (°C) <sup>e</sup>
1			
Si-doped GaAs (upper)	0.20	$2.0\times10^{18}$	610
Si-doped GaAs (middle)	1.80	$2.0 \times 10^{18}$	695
Semi-insulating GaAs (substrate)	<b>400</b> .0		
2			
Si-doped GaAs (upper)	0.20	$2.0 \times 10^{16}$	610
Si-doped GaAs (middle)	2.80	$2.0 \times 10^{16}$	695
Semi-insulating GaAs (substrate)	400.0		
3			
Si-doped GaAs (upper)	0.25	$3.6 \times 10^{14}$	580
Si-doped GaAs (middle)	10.0	$3.6 \times 10^{14}$	630
Semi-insulating GaAs (substrate)	400.0		
4			
Be-doped GaAs (upper)	0.20	$2.0 \times 10^{18d}$	610
Be-doped GaAs (mid- dle)	1.80	$2.0 \times 10^{16d}$	695
Semi-insulating GaAs (substrate)	400.0		

<sup>&</sup>quot;Thickness of layer

dHole concentration (p).

picted in Fig. 2. The sample was placed horizontally at the bottom of a quartz cuvette with dimensions 10 mm  $\times$  10 mm  $\times$  40 mm, and CCl<sub>4</sub> is added to the cuvette to a height of  $\sim$ 10 mm above the sample surface. The argon-ion laser beam was focused upon the sample surface by a convex lens of 20-cm focal length. The pump-beam spot size at the sample surface was estimated to be 102  $\mu$ m. The mirror and the lens (L<sub>1</sub>, Fig. 2) were fixed on an xy translator, and the translator is positioned in such a way that the center of the mirror, the lens, and the cuvette are in a vertical line, the z axis. In this experimental arrangement one can accurately vary the pump-

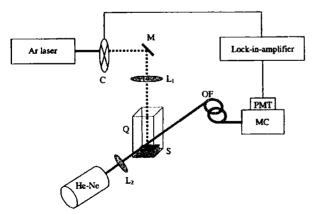


Fig. 2. Schematic view of the experimental setup: M, mirror; C, chopper; L<sub>1</sub>, L<sub>2</sub>, lenses; Q, cuvette; S, sample; OF, optical fiber; MC, monochromator; PMT, photomultiplier tube.

beam's position on the sample along the x directions simply moving the translator in the x directions mechanical chopper (Stanford Research System Model SR540) was placed in the pump-beam paths modulate the pump beam's intensity at the desire frequency.

A 3-mW He-Ne laser (Spectra-Physics) emitting 632.8 nm was used as the probe beam to detect strength of the refractive-index gradient generated: CCl<sub>4</sub>. The probe laser beam had a Gaussian prowith a  $(1/e^2)$  diameter of 800  $\mu$ m and was focused a convex lens of 10-cm focal length. The probe beam's spot size at the point where it crosses a pump beam was estimated to be 101  $\mu$ m. The probable was arranged such that it just skinner through the surface of the sample, and it propagation a direction (y axis) orthogonal to that of the part beam (z axis).

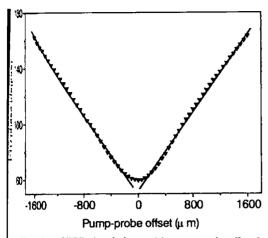
A plastic fiber with a circular core of 1-mm de eter was used as a position-sensitive detector to ma itor the periodic deflection of the probe beam. In end of the fiber was firmly fixed upon an xyz me lator at a distance of 15 cm from the sample 1 other end of the fiber was coupled to a 0.25-m man chromator (McPherson) tuned to the probe bear wavelength. A photomultiplier tube was coupled the exit slit of the monochromator. The output the photomultiplier tube was fed to a dual-phase to ital lock-in-amplifier (Stanford Research Symm Model SR830) through an impedance-matching The entire experimental setup was laid out a moderately vibration-isolated table to protect \$ system from ambient vibrations. Measurement were carried out at a pump-beam modulation b quency of 10.6 Hz, and the distance between a probe beam height and the sample surface was in as small as possible to produce a nondiffracted in the sample edge) probe beam at the detector.

# 4. Results and Discussion

Measurements were carried out by irradiation of thin-film sides as well as of the substrate sides di samples. In the present experiment the pri beam, the position-sensitive detector, and the were firmly fixed at specific positions and the pas beam irradiation site on the sample surface was we ied across the probe beam. A typical variation of signal phase with the pump-probe offset for same when the semi-insulating GaAs substrate side is ing the pump beam is shown in Fig. 3. Them mum in the phase plot corresponds to zero de Identical signal profiles were observed for the a strates of other samples also. From the slope either side of the plot the thermal diffusivity da substrate was evaluated by use of the relation gives Eq. (6). The measured values of  $\alpha$ , calculated in the average of the two slopes, are listed in Table Almost identical a values obtained for the substract all the four samples indicate that the epitaxial and grown upon the other surfaces of the substrates but significant influence on the PTD signal generated the substrate. The literature values of a of Galai

<sup>&</sup>lt;sup>b</sup>Electron concentration.

<sup>&#</sup>x27;Substrate temperature at which the layers are grown.



1) Variation of PTD signal phase with pump–probe offset for 1 (substrate-side illumination).

the range 0.2–0.36 cm² s<sup>-1</sup>, <sup>14</sup>, <sup>20</sup>–<sup>25</sup> and the experisally observed values also fall within this range. It wide range of a values reported in the literature is to the large variation of thermal transport proposof semiconductor materials with the growth continuous defects, etc. In the case of a semi-insulating monductor, the free-carrier density is low and are similarly to the heat conduction in dielectrics, whomous make the main contribution to heat transfin these materials. <sup>25</sup>, <sup>26</sup>

figure 4 shows the variation of PTD signal phase with pump-probe offset for sample 1 when the zefilm side is facing the pump beam. Again, the amal diffusivities of the films were evaluated from \*slope of the plot, and the average values of the resured a are listed in Table 2. To explain the aresting results obtained from the epitaxial layers need to recollect some of the fundamental facts garding heat conduction in semiconductors. In monductor samples, in addition to the pure therwave effect, electronic diffusion and carrier remination, may also contribute to the PTD signal. appre thermal wave component of the PTD signal see from the instantaneous intraband electronmon interaction and the subsequent phonon msport. For an extrinsic semiconductor, in addino the contribution by free carriers, a nonradiamecombination of the photoexcited carriers that ndiffused through the sample may also contribute

in 2 Thermal Diffusivity Values of GaAs Multilayers Evaluated from the Photothermal Beam Deflection Measurements

	Thermal diffusivity $\alpha$ (cm <sup>2</sup> s <sup>-1</sup> )		
imple Number	Film-Side Illumination	Substrate-Side Illumination	
1	0.193	0.212	
2	0.187	0.212	
3	0.165	0.210	
4	0.160	0.206	

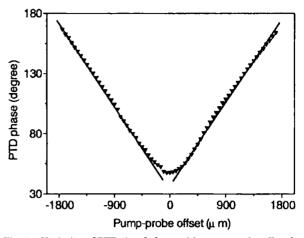


Fig. 4. Variation of PTD signal phase with pump-probe offset for sample 1 (film-side illumination).

to the heat transport. Fournier et al. made a rigorous theoretical and experimental analysis in this regard and proved that, at very low frequencies, i.e., when  $\omega \tau \ll 1$ , only the pure thermal wave component contributes to the PTD signal; consequently the signal's behavior (both amplitude and phase) is characterized by the thermal diffusivity of the sample.<sup>27</sup> Here,  $\omega = 2\pi f$ , where f is the pump beam's modulation frequency and  $\tau$  is the photoexcited carrier recombination lifetime. When the pump beam's modulation time scale is much shorter than T, however, i.e., when  $\omega\tau\gg$  1, the contribution from the pure thermal wave component drops off, and recombination processes now dominate the PTD signal. In this regime the signal behavior is characterized by electronic diffusivity. Usually,  $\tau$  for n-type GaAs is of the order of microseconds, and for p-type GaAs it is as low as nanoseconds.20-22 Hence at a modulation frequency of 10.6 Hz the contributions from photoexcited carrier recombination are expected to be negligible. Furthermore, it is clear from Fig. 4 that Eq. (6) holds in the case of epitaxial layers also, in agreement with the previous statement that the contribution from photoexcited carrier recombination is negligible.

The excitation photon energy, 2.54 eV, is much greater than the bandgap energy of GaAs (1.43 eV), and the entire energy is absorbed at the surface ( $\sim 1$ µm) of the epitaxial layer itself. Consequently the samples are optically opaque at the excitation wavelength. Moreover, the fact that the entire energy is absorbed at the surface of the sample implies that heat is generated in the surface epitaxial layer but propagates through the entire structure. Nevertheless, the decrease of a values of the epitaxial layers compared with the bulk diffusivity value suggests some interesting but complex heat transport mechanisms in these samples. The increase in the number of scattering centers that resulted from doping of GaAs with either Si or Be and the consequent reduction of the phonon mean free path do not seem to be the only reasons for the noticeable reduction in the diffusivity values of the epitaxial layers. Recently a number of research papers reported the experimental observation of substantial reduction (as much as 50%) in lattice thermal conductivity in semiconductor thin films, especially when the thin-film thickness was of the order of the phonon's mean free path.  $^{20,28-31}$  But the exact values of the phonon's mean free path of the samples investigated here are not available for detailed analysis. According to the kinetic theory the phonon's mean free path in the bulk sample  $\Lambda_{\rm bulk}$  can be evaluated from the relation

$$\Lambda_{\text{bulk}} = 3k_{\text{bulk}}/C\nu, \tag{7}$$

where  $k_{\text{bulk}}$  is the bulk thermal conductivity, C is the volumetric heat capacity, and  $\nu$  is the speed of sound in the material. For bulk GaAs,  $k_{\rm bulk} = 0.46 \, \rm W/(cm/^{\circ}C)$ ,  $C = 0.33 \, \rm J(g/^{\circ}C)$ , and  $\nu \approx 4.0 \times 10^{5} \, \rm cm/s$ , which lead to the estimation of a phonon mean free path of approximately 100 nm.20-22 This value is smaller than those of the surface layer thicknesses 200 and 250 nm, of the samples. However, the estimated value of the phonon's mean free path need not be strictly true, because there is a large discrepancy between the experimentally observed value of the phonon's mean free path and that evaluated theoretically; hence it is hard to analyze the observed thermal diffusivity data without knowing the exact value of  $\Lambda_{\text{bulk}}$ . For example, in a recent paper Ju and Goodson measured the effective phonon mean free path in Si as 300 nm, whereas that evaluated by the kinetic theory is only 43 nm.28 But an important point to be mentioned is that the thicknesses of the thin films are too small compared with the thermal diffusion length and hence the tabulated thermal diffusivity value may be the effective diffusivity of the thin films and that of the substrate. However, a general conclusion that can be drawn from the tabulated thermal diffusivity values is that, for samples 1-3, all doped with Si, the trend is for a decrease in thermal diffusivity with a decrease in doping density and an increase in thickness of the second (under) epitaxial layer. Also, for sample 4, which is doped with Be, the diffusivity value is smaller than that of the corresponding n-type sample (sample 1).

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