Microwave dielectric properties of $MO-La_2O_3-TiO_2$ (M = Ca, Sr, Ba) ceramics

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Single-phase polycrystalline ceramics in the MO-La₂O₃-TiO₂ (M = Ca, Sr, Ba) system, such as cation-deficient hexagonal perovskites CaLa₄Ti₄O₁₅, SrLa₄Ti₄O₁₅, BaLa₄Ti₄O₁₅, and Ca₂La₄Ti₅O₁₈ and the orthorhombic phases CaLa₄Ti₅O₁₇ and CaLa₈Ti₉O₃₁, were prepared through the solid-state ceramic route. The phases and structure of the ceramics were analyzed through x-ray diffraction and scanning electron microscopy. The microwave dielectric properties of the ceramics were studied using a network analyzer. The investigated ceramics show high ϵ_r in the range 42 to 54, high quality factors with $Q \times f$ in the range 16,222 to 50,215 GHz, and low τ_f in the range -25 to +6 ppm/°C. These high dielectric constant materials with high $Q \times f$ up to 50,215 GHz are suitable for applications where narrow bandwidth and extremely low insertion loss is necessary, especially at frequencies around 1.9 GHz.

I. INTRODUCTION

The dramatic advancements during the last two decades in the microwave integrated circuit technology have brought a revolution in telecommunication systems. Dielectric resonators (DRs) provide a compact, low-cost, and highly reliable choice as resonator elements in microwave circuits, and they now replace the conventional metallic cavity and microstrip resonators more frequently than ever before. The size of the microwave circuit is inversely proportional to the square root of its dielectric constant. The constraints due to size, frequency of operation, frequency stability, and selectivity allow only those materials with high dielectric constant (20–100), high *Q* factor (>2000), and low temperature coefficient of resonant frequency ($\tau_f < \pm 20$ ppm/°C) for DR applications.

Most of the commercial DRs available at present fall into two groups: (i) ceramics with low dielectric constant $(20 < \epsilon_r < 40)$ and high Q factor $(Q \times f > 50,000 \text{ GHz})$ such as Ba $(Mg_{1/3}Ta_{2/3})O_3$, Ba $(Zn_{1/3}Ta_{2/3})O_3$, their solidsolution modifications, Ba₂Ti₉O₂₀, (Zr,Sn)TiO₄, etc.; (ii) ceramics with high dielectric constant (>65) and low Qfactor ($Q \times f < 10,000$), such as the tungsten-bronze type materials in the BaO-RE₂O₃-TiO₂ system. Though high dielectric constant materials can give better miniaturization, the applications requiring narrow bandwidth and extremely low insertion loss (0.3 dB) enables the use of ceramics having even $\epsilon_r = 38$.¹ Dielectric materials with $\epsilon_r > 40$ and $Q \times f > 45,000$ GHz can allow for further miniaturization of the devices without much compromise in quality. Materials with ϵ_r in the range 40 to 65 suitable for such applications are few, and the search for such materials is one of the current areas of research in microwave dielectrics. The Ba₅Nb₄O₁₅type cation-deficient hexagonal perovskites are characterized by high dielectric constant and high quality factor. The microwave dielectric properties of Ba₅Nb₄O₁₅, $Ba_{5-x}Sr_{x}Nb_{4}O_{15}$, $Ba_{5}Ta_{4}O_{15}$, and $(Ba,La)_{n}Ti_{n-1}O_{3n}$ (n = 5, 6) have already been reported.²⁻⁶ The ceramics are characterized by high dielectric constants up to 50.6 and $Q \times f$ up to 44,000 GHz. Veneis et al.³ reported the microwave dielectric properties of BaLa4Ti4O15 and Ba₂La₄Ti₅O₁₈, and the ceramics show high dielectric constants and quality factors with small temperature coefficients of resonant frequency.³ In the present paper, we report the preparation, characterization, and microwave dielectric properties of the cation-deficient hexagonal phases $(M,La)_n Ti_{n-1}O_{3n}$ (M = Ca, Sr, Ba; n = 5, 6) and the orthorhombic type CaLa₄Ti₅O₁₇, Ca₂La₄Ti₆O₂₀, and CaLa₈Ti₉O₃₁ ceramics belonging to the CaO-La₂O₃-TiO₂ system. The microwave dielectric properties of the Ca- and Sr-based ceramics are reported for the first time.

The $(M,La)_n Ti_{n-1}O_{3n}$ (M = Ca, Sr, Ba; n = 5, 6) ceramics, i.e., CaLa₄Ti₄O₁₅, SrLa₄Ti₄O₁₅, BaLa₄Ti₄O₁₅, and Ca₂La₄Ti₅O₁₈, crystallize in a hexagonal

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structure.⁷⁻¹² The above compounds belong to the cation-deficient hexagonal perovskite family $A_n B_{n-1} O_{3n}$ (n = 5, 6, or 8) where the M and La ions occupy the A sites, and Ti ions occupy the B sites. The crystal lattice of the cation-deficient perovskite-related phases $A_n B_{n-1} O_{3n}$ (n = 5, 6, 8) can be derived from the basic perovskite structure by the periodic introduction of intrinsic stacking faults in the cubic close packing of the AO3 mixed lavers with hexagonal structure. Alternatively, the structure may be defined as consisting of identical perovskite like blocks of n corner sharing octahedra where successive blocks are shifted by $\frac{1}{3}\langle 10\overline{1}0\rangle$ vector. One *n*th of the octahedral holes are kept vacant in such a way that B cations are omitted from the face sharing octahedral holes to form the cation-deficient structure. The A site ions are 12-fold coordinated whereas B site ions are 6-fold coordinated. The lattice parameters and the atom positions of the homologous phases BaLa₄Ti₄O₁₅ and Ba2La4Ti5O18 were precisely determined by Harre et al.^{10,11} based on single-crystal x-ray diffraction (XRD) and later confirmed by neutron diffraction studies.¹²

II. PREPARATION AND CHARACTERIZATION

The ceramics were prepared through the solid-state ceramic route. High-purity CaCO₃ (99+%), BaCO₃ (99+%), and SrCO₃ (99.9%), and TiO₂ (99.9%) (Aldrich Chemicals Company, Inc., Milwaukee, WI) were used as the starting oxide powders. La2O3 (99.99%, Indian Rare Earths, Kerala, India) was heated at 1000 °C for 3 h before weighing to remove any hydroxides. The powders were weighed according to the stoichiometry and ball milled in distilled water medium for 24 h in a plastic bottle using zirconia balls. The wet mixed powder was dried and calcined at 1200 °C for 4 h, then ground and again calcined at 1400-1450 °C for 4 h. The calcined mixture was ground well. Then 3 wt% PVA was added as the binder, the powder was mixed, dried, and again ground. The resultant fine powder was uniaxially pressed in a tungsten carbide die under a pressure of 150 MPa such that the pressed disks were 6-8 mm high and 14 mm in diameter. Stearic acid was used as a lubricant. The green pellets were sintered at different temperatures in the range 1500-1675 °C for 4 h. The sintering temperatures were optimized for maximum density. The sintered samples were typically annealed at 1400-1450 °C for 12 h to minimize the reduction of titanium ions. The sintered pellets were polished well, and the bulk densities were measured using the Archimedes method. The phase purity of the sintered samples was studied by XRD using a Rigaku x-ray diffractometer (Dmak 1C, Tokyo, Japan). The surface morphology of the samples was studied using scanning electron microscopy (SEM). The sintered samples were thermally etched at temperatures 50 °C lower than their respective sintering temperature for 30 min and were used for recording SEM.

The microwave dielectric properties were measured using an HP 8510C network analyzer (Hewlett-Packard, Palo Alto, CA). The microwave dielectric constant was measured by the dielectric post resonator method suggested by Hakki and Coleman and modified by Courtney.^{13,14} The resonator was placed between two goldcoated copper metallic plates, and microwave energy was coupled through E-field probes to excite various resonant modes. Among the various resonant modes, the TE₀₁₁ mode was selected for the measurement. The quality factors of the samples were measured at the TE018 mode resonant frequency using a transmission mode cavity.¹⁵ The temperature coefficient of resonant frequency (τ_f) was measured from the slope of the graph plotted between resonant frequency and temperature. The measurement is usually done in the range 20-80 °C.

III. RESULTS AND DISCUSSION

The ceramics were sintered into dense bodies. The percentage densities of the sintered samples are given in Table I. The MaLa₄Ti₄O₁₅ (M = Ca, Sr, Ba) ceramics show densities in the range 95–98% of their theoretical densities, whereas Ca₂La₄Ti₅O₁₈ shows only 93.6% of its theoretical density. The CaLa₄Ti₅O₁₇ and CaLa₈Ti₉O₃₁ were densified to 98.2% and 92.1% of their respective theoretical densities. The BaLa₄Ti₄O₁₅ ceramic was sintered well at 1550 °C for 4 h, whereas its strontium counterpart was sintered well at 1625 °C for 2 h. The calcium-based compounds were sintered into dense bodies in the temperature range 1650–1670 °C for 4 h.

A. XRD and SEM analysis

The XRD patterns recorded for the ceramics were compared with standard data.¹⁶ The XRD patterns of the MLa₄Ti₄O₁₅ (M = Ca, Sr, Ba) and Ca₂La₄Ti₅O₁₈ ceramics are shown in Fig. 1, and those of the orthorhombic CaLa₄Ti₅O₁₇ and CaLa₈Ti₉O₃₁ are shown in Fig. 2. The obtained compounds were phase pure. The CaLa₄Ti₄O₁₅, BaLa₄Ti₄O₁₅, and SrLa₄Ti₄O₁₅ ceramics

TABLE I. Microwave dielectric properties of $MO-La_2O_3-TiO_2$ ceramics (M = Ca, Sr, Ba).

Material	Percentage density	¢ _r	ϵ_r (corrected)	$ au_{f}$ (ppm/°C)	Q ₀	f (GHz)	$Q_0 \times f$ (GHz)
CaLa, Ti, O, s	95.2	41.6	44.7	-25	8100	4.31	34911
SrLa Ti Ois	98.0	43.8	45.1	-14	12100	4.15	50215
BaLa, Ti, O,	96.2	46.3	49.1	-13	3150	5.15	16222
Ca-La Ti-O10	93.6	44.7	49.3	+6	4800	4.19	20112
CaLa Ti O17	98.2	53.7	55.2	-20	4730	3.67	17359
CaLa ₈ Ti ₉ O ₃₁	92.1	48.6	54.9	-6	5300	3.65	19345

crystallized in a hexagonal structure, and the close similarity of their XRD patterns is well evident in Fig. 1. The calculated lattice parameters were found to agree closely with the reported values. The pattern recorded for $BaLa_4Ti_4O_{15}$ was indexed by doubling the unit cell along the c axis to account for some very weak maxima in the pattern so that the unit cell contains ten perovskite layers.^{7,10,12} SrLa₄Ti₄O₁₅ crystallizes in the hexagonal structure with hhccc stacking.⁸ CaLa₄Ti₄O₁₅ belongs to $A_5B_4O_{15}$ with *hccch* stacking $(p\bar{3}m)$, and $Ca_2La_4Ti_5O_{18}$ belongs to A₆B₅O₁₈ with hcccchhcccchh stacking [R3m] and crystallizes within the trigonal system with $Z = 3.9 A_n B_{n-1} O_{3n}$ compounds usually show a severe distortion of TiO₆ octahedra and the presence of short Ti-O bonds. The decrease in difference between charges of the cations reduces the effect of ordering on the stability of the structure and hence a distorted distribution of the Ca and La cations is found in Ca₂La₄Ti₅O₁₈.⁹ Especially in those cases where hexagonal polytypes of the perovskites are also possible for ABO₃, the stability of phases with an ordered distribution of vacancies decreases as the Goldschmidt "t" criterion¹⁷ increases and above 1450 °C the hexagonal A₆B₅O₁₈ phases



FIG. 1. X-ray diffraction patterns of (a) $BaLa_4Ti_4O_{15}$, (b) $SrLa_4Ti_4O_{15}$, (c) $CaLa_4Ti_4O_{15}$, and (d) $Ca_2La_4Ti_5O_{18}$.

decompose slowly in the solid state.⁹ Figure 3 shows typical SEM pictures recorded for $BaLa_4Ti_4O_{15}$ and $CaLa_4Ti_5O_{17}$. The $BaLa_4Ti_4O_{15}$ grains are elongated and up to about 10 µm in length. The $CaLa_4Ti_5O_{17}$ grains are large and up to 15 µm in size. Other samples also showed similar microstructures. The SEM pictures confirmed the single-phase nature of the compounds. The near-to-melting appearance of the ceramics [Fig. 3(b)] may be due to higher sintering temperatures. These DR samples are optimized to have the best Q at these temperatures.

B. Microwave dielectric properties

The ceramics showed excellent microwave dielectric properties. The TE₀₁₈ modes of the samples were obtained in the range of 4-6 GHz. The microwave dielectric properties of the ceramics are given in Table I. The variation of $(\Delta f/f)$ with temperature for the compounds is given in Fig. 4. The BaLa₄Ti₄O₁₅ shows $\epsilon_r = 46.3$ and $\tau_f = -13 \text{ ppm/}^{\circ}\text{C}$ with quality factor of 3150 (at 5.15 GHz) for 96.2% dense samples. Veneis et al. have reported that BaLa₄Ti₄O₁₅ has ϵ_r of 43 and Q of 1430 (at 8.10 GHz) with τ_f of -17 ppm/°C for 93.7% dense ceramics.³ The higher densification of the present ceramic may be the reason for the increase in dielectric constant and quality factor of the ceramics. The SrLa₄Ti₄O₁₅ ceramics had ϵ_r of 43.8 with very high Q factor of 12,100 (at 4.149 GHz) and a low τ_f of -14 ppm/°C. Ca₂La₄Ti₅O₁₈ showed a quality factor of 4800 at 4.19 GHz whereas it was 8100 at 4.31 GHz for CaLa₄Ti₄O₁₅. German and Kovba have reported that Ca₂La₄Ti₅O₁₈ has a more diffuse infrared and Raman



FIG. 2. X-ray diffraction patterns of (a) $CaLa_4Ti_5O_{17}$ and (b) $CaLa_8Ti_9O_{31}.$





(b)

FIG. 3. SEM pictures recorded for (a) $BaLa_4Ti_4O_{15}$ and (b) $CaLa_4Ti_5O_{17}.$



FIG. 4. Plot of $\Delta f/f$ against temperature (a) SrLa₄Ti₄O₁₅, (b) CaLa₄Ti₄O₁₅, (c) Ca₂La₄Ti₅O₁₈, (d) Ca₂La₄Ti₅O₁₇, and (e) CaLa₈Ti₉O₃₁.

spectra than CaLa₄Ti₄O₁₅.⁹ They have suggested a distorted distribution of the Ca and La cation among the equivalent positions to interpret the spectra. This statistical distribution and the resultant disorder of the Ca and La ions may cause lower quality factors of the Ca₂La₄Ti₅O₁₈ compared to CaLa₄Ti₄O₁₅ apart from the higher porosity. Usually the broadening of the Raman spectra indicates disorder in crystals.¹⁸ The orthorhombic CaLa₄Ti₅O₁₇ and CaLa₈Ti₉O₃₁ were also characterized by very good microwave dielectric properties with ϵ_r of 53.7 and 48.6, quality factors of 4730 (at 3.67 GHz) and 5300 (at 3.65 GHz) and low τ_f of -20 and -6 ppm/°C, respectively. Ca₂La₄Ti₆O₂₀ showed poor resonance due to very high dielectric loss and is therefore not useful for DR applications.

The values of the microwave dielectric constant obtained for the ceramics were corrected for porosity (refer to Table II) using the following equation:¹⁹

$$\dot{\epsilon} = \epsilon_{\rm m} \left(1 - \frac{3P(\epsilon_{\rm m} - 1)}{2\epsilon_{\rm m} + 1} \right)$$

where ϵ_m is the dielectric constant corrected for porosity, ϵ' is the experimental dielectric constant, and *P* is the fractional porosity. The dielectric constant is calculated using the Clausius-Mossotti equation:

$$v_r = \frac{3V_m + 8\pi\alpha_D}{3V_m - 4\pi\alpha_D}$$

where $V_{\rm m}$ is the molar volume and $\alpha_{\rm D}$ is the sum of ionic polarizabilities of individual ions. The calculated dielectric constants usually agree well with the experimental values for well-behaved ceramics.^{20,21} However, an inconsistency is found when the equation is applied to the La containing BaLa₄Ti₄O₁₅ and Ba₂La₄Ti₅O₁₈ ceramics.³ It has been suggested that if the ionic polarizability of La ion is changed to 4.82 instead of 6.12, given by Shannon, this inconsistency can be avoided.³ We calculated the dielectric constant of the investigated materials using $\alpha_{La} = 4.82$. The calculated and experimental dielectric constants (after applying porosity correction) for the ceramics are given in Table II. The deviations of the calculated values from the experimental values are also given in Table II. There is reasonable agreement between the calculated and experimental values. The small differences between calculated and experimental values are due to deviations from the cubic symmetry and also the fact that the sample is a ceramic and not a single crystal. The calculated values show significant difference from the experimental values for Ca2La4Ti5O18, CaLa₄Ti₅O₁₇, and CaLa₈Ti₉O₃₁. It may be noted that the equation used for the calculation of dielectric constant is highly sensitive to the value of the denominator, and even a small error in determining the cell volume can

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Material	$\alpha_{\rm D} \; (\alpha_{\rm La} = 4.82)$	$V_{\rm m}$ (Å ³)	Space group	ϵ_r (corrected)	Calculated ϵ_r	Deviation (%)
CaLa ₄ Ti ₄ O ₁₅	64.31	291.98	P3m	44.7	36.74	17.4
SrLa, Ti, O, s	65.39	295.22	P3m	45.1	39.53	12.4
BaLaTiO	67.55	302.48	P3m	49.1	44.45	9.5
Ca_La_Ti_O18	76.43	349.5	R3m	49.3	33.71	31.6
CaLa ₄ Ti ₅ O ₁₇	72.34	336.43	Windig	55.2	28.2	48.9
CaLa ₈ Ti ₉ O ₃₁	131.48	613.47	loten, Res., 19, astol	54.9	27.34	50.0

TABLE II. Comparison of values of experimental and calculated dielectric constants.



FIG. 5. Variation of ϵ_r and τ_f with average ionic radius of A site ion for MLa₄Ti₄O₁₅.

significantly affect the calculated value of dielectric constant. Figure 5 shows the variation of the porositycorrected dielectric constant and temperature coefficient of resonant frequency with average ionic radius of the A site ions for the $MLa_4Ti_4O_{15}$ (M = Ca, Sr, Ba) system. The dielectric constant of the materials in the system increases with the average ionic radius of the A site ions.

We investigated phase formation within the compositions $\text{SrO}-2\text{RE}_2\text{O}_3-4\text{TiO}_2$ (RE = Sm, Nd, Pr, and Gd). The mixed oxide powders are calcined in the range 1350–1500 °C for 4 to 8 h and sintered at 1625–1650 °C for 4 h. No cation-deficient hexagonal phases analogous to $\text{SrLa}_4\text{Ti}_4\text{O}_{15}$ compounds were found. The compositions show a multiphase appearance and mostly contain the $\text{RE}_2\text{Ti}_2\text{O}_7$ pyrochlores. The ceramics show good microwave dielectric properties except $\text{SrO}-2\text{Gd}_2\text{O}_3-\text{TiO}_2$ ceramics, which have poor resonance due to high dielectric loss. The phase formation within the investigated compositions was found to be sensitive to the preparation conditions, and different batches of the ceramics show variation in microwave dielectric properties.

Among the investigated cation-deficient hexagonal perovskites, only Ca₂La₄Ti₅O₁₈ showed a positive value of $\tau_{\rm f}$ (+6 ppm/°C). The investigated ceramics showed dielectric constant in the range 42–54 and high $Q \times f$ in the range 16,222–50,215 GHz with a low temperature coefficient of resonant frequency in the range +6 to -25 ppm/°C. The investigated ceramics are potential

candidates for practical applications. These high dielectric constant materials with high $Q \times f$ up to 50,215 GHz are suitable for applications where narrow bandwidth and extremely low insertion loss is necessary, especially at frequencies around 1.9 GHz.

IV. CONCLUSION

Cation-deficient hexagonal perovskites CaLa₄Ti₄O₁₅, SrLa₄Ti₄O₁₅, BaLa₄Ti₄O₁₅, and Ca₂La₄Ti₅O₁₈ and the orthorhombic phases CaLa₄Ti₅O₁₇ and CaLa₈Ti₉O₃₁ were prepared through the solid-state ceramic route. The phases and structure of the ceramics were analyzed through XRD and SEM. The microwave dielectric properties of the ceramics were studied. The ceramics showed high ϵ_r in the range 42–54, high quality factors with $Q \times f$ in the range 16,222–50,215 GHz, and low τ_f in the range of -25 and +6 ppm/°C. Their high dielectric constants and high quality factors of $Q \times f$ up to 50,215 GHz with low temperature coefficients of resonant frequency make them suitable for applications where narrow bandwidth and extremely low insertion loss are necessary, especially at frequencies around 1.9 GHz.

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